

Solving Linear Equations

To determine whether a value is a solution of an equation, substitute the value into the equation and simplify.

Example 1 Determine whether (a) $x = 1$ or (b) $x = -2$ is a solution of $5x - 1 = 4$.

a. $5x - 1 = -2x + 6$

$$5(1) - 1 \stackrel{?}{=} -2(1) + 6$$

Substitute.

$$4 = 4 \quad \checkmark$$

Simplify.

b. $5x - 1 = -2x + 6$

$$5(-2) - 1 \stackrel{?}{=} -2(-2) + 6$$

Substitute.

$$-11 \neq 10 \quad \times$$

Simplify.

► So, $x = 1$ is a solution.

► So, $x = -2$ is *not* a solution.

To solve a linear equation, isolate the variable.

Example 2 Solve each equation. Check your solution.

a. $4x - 3 = 13$

$$\begin{aligned} 4x - 3 &+ 3 = 13 + 3 && \text{Add 3.} \\ 4x &= 16 && \text{Simplify.} \\ \frac{4x}{4} &= \frac{16}{4} && \text{Divide by 4.} \\ x &= 4 && \text{Simplify.} \end{aligned}$$

b. $2(y - 8) = y + 6$

$$\begin{aligned} 2y - 16 &= y + 6 && \text{Distributive Property} \\ 2y - y - 16 &= y - y + 6 && \text{Subtract } y. \\ y - 16 &= 6 && \text{Simplify.} \\ y - 16 + 16 &= 6 + 16 && \text{Add 16.} \\ y &= 22 && \text{Simplify.} \end{aligned}$$

Check

$$\begin{aligned} 4x - 3 &= 13 \\ 4(4) - 3 &\stackrel{?}{=} 13 \\ 13 &= 13 \quad \checkmark \end{aligned}$$

Check

$$\begin{aligned} 2(y - 8) &= y + 6 \\ 2(22 - 8) &\stackrel{?}{=} 22 + 6 \\ 28 &= 28 \quad \checkmark \end{aligned}$$

Practice

Check your answers at BigIdeasMath.com.

Determine whether (a) $x = -1$ or (b) $x = 3$ is a solution of the equation.

1. $5x + 7 = 2$

2. $-4x + 8 = -4$

3. $2x - 1 = 3x - 4$

Solve the equation. Check your solution.

4. $x - 9 = 24$

5. $n + 14 = 0$

6. $-16 = 4y$

7. $-\frac{5}{6}t = -15$

8. $81 = 46 - x$

9. $4x + 5 = 1$

10. $x + 5 = 11x$

11. $9(y - 3) = 45$

12. $6 = 7k + 8 - k$

13. $6n + 3 = -4n + 7$

14. $2c + 5 = 3(c - 8)$

15. $18m + 3(2m + 8) = 0$

16. $\frac{w - 6}{5} = 8$

17. $\frac{15 + h}{3} = 10$

18. $\frac{8 - 3x}{5} = x$

19. $(8r + 6) + (4r - 1) = 14$

20. $\frac{2}{3}y - 3 = 9$

21. $\frac{1}{2}x - \frac{3}{10} = \frac{5}{2}x + \frac{7}{10}$

22. **MONEY** You have a total of \$3.25 in change made up of 25 pennies, 6 nickels, 2 dimes, and x quarters. How many quarters do you have?