

Multiplying and Dividing Fractions

To multiply two fractions, multiply the numerators and multiply the denominators.

Multiplying Fractions
$\frac{a}{b} \cdot \frac{c}{d} = \frac{a \cdot c}{b \cdot d}$, where $b, d \neq 0$

Example 1 Find $\frac{2}{5} \cdot \frac{3}{8}$.

$$\begin{aligned} \frac{2}{5} \cdot \frac{3}{8} &= \frac{2 \cdot 3}{5 \cdot 8} && \text{Multiply the numerators.} \\ & && \text{Multiply the denominators.} \\ &= \frac{\overset{1}{\cancel{2}} \cdot 3}{8 \cdot \underset{4}{\cancel{8}}} && \text{Divide out common factors.} \\ &= \frac{3}{20} && \text{Simplify.} \end{aligned}$$

Example 2 Find $5\frac{1}{2} \cdot \frac{3}{4}$.

$$\begin{aligned} 5\frac{1}{2} \cdot \frac{3}{4} &= \frac{11}{2} \cdot \frac{3}{4} && \text{Rewrite } 5\frac{1}{2} \text{ as } \frac{11}{2}. \\ &= \frac{11 \cdot 3}{2 \cdot 4} && \text{Multiply the numerators.} \\ & && \text{Multiply the denominators.} \\ &= \frac{33}{8}, \text{ or } 4\frac{1}{8} && \text{Simplify.} \end{aligned}$$

Two numbers whose product is 1 are **reciprocals**. To write the reciprocal of a number, write the number as a fraction. Then invert the fraction. Every number except 0 has a reciprocal.

To divide a number by a fraction, multiply the number by the reciprocal of the fraction.

Dividing Fractions
$\frac{a}{b} \div \frac{c}{d} = \frac{a}{b} \cdot \frac{d}{c} = \frac{a \cdot d}{b \cdot c}$, where $b, c, d \neq 0$

Example 3 Find $\frac{3}{7} \div \frac{5}{6}$.

$$\begin{aligned} \frac{3}{7} \div \frac{5}{6} &= \frac{3}{7} \cdot \frac{6}{5} && \text{Multiply by the reciprocal} \\ & && \text{of } \frac{5}{6}, \text{ which is } \frac{6}{5}. \\ &= \frac{3 \cdot 6}{7 \cdot 5} && \text{Multiply.} \\ &= \frac{18}{35} && \text{Simplify.} \end{aligned}$$

Example 4 Find $8 \div 2\frac{1}{3}$.

$$\begin{aligned} 8 \div 2\frac{1}{3} &= 8 \div \frac{7}{3} && \text{Rewrite } 2\frac{1}{3} \text{ as } \frac{7}{3}. \\ &= 8 \cdot \frac{3}{7} && \text{Multiply by the reciprocal} \\ & && \text{of } \frac{7}{3}, \text{ which is } \frac{3}{7}. \\ &= \frac{8 \cdot 3}{7} && \text{Multiply.} \\ &= \frac{24}{7}, \text{ or } 3\frac{3}{7} && \text{Simplify.} \end{aligned}$$

Practice

Check your answers at BigIdeasMath.com.

Write the reciprocal of the number.

1. $\frac{3}{8}$ 2. 7 3. -12 4. $-\frac{6}{5}$

Evaluate.

5. $\frac{3}{4} \cdot \frac{1}{6}$ 6. $\frac{3}{10} \cdot \frac{2}{3}$ 7. $\frac{4}{9} \cdot \frac{2}{9}$ 8. $\frac{5}{8} \cdot \frac{7}{12}$
9. $4 \cdot \frac{3}{16}$ 10. $3\frac{1}{2} \cdot \frac{6}{7}$ 11. $1\frac{7}{20} \cdot 2\frac{4}{5}$ 12. $\frac{1}{10} \cdot 10$
13. $\frac{1}{6} \div \frac{1}{2}$ 14. $\frac{7}{8} \div \frac{7}{8}$ 15. $\frac{9}{10} \div \frac{3}{5}$ 16. $\frac{3}{4} \div \frac{5}{8}$
17. $18 \div \frac{2}{3}$ 18. $7\frac{1}{2} \div 2\frac{1}{10}$ 19. $6\frac{3}{7} \div 3$ 20. $1\frac{3}{25} \div \frac{1}{5}$

21. **AREA** Find the area of a rectangular court that is $21\frac{3}{5}$ meters long and $13\frac{3}{4}$ meters wide.

22. **CARPENTRY** How many $1\frac{1}{4}$ -foot pieces can you cut from a piece of wood that is 20 feet long?