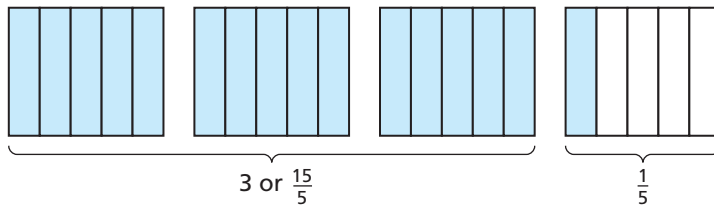


Mixed Numbers and Improper Fractions

A **mixed number** is the sum of a whole number and a fraction. An **improper fraction** is a fraction with a numerator that is greater than or equal to the denominator.

The shaded part of the model represents the mixed number $3\frac{1}{5}$ and the improper fraction $\frac{16}{5}$.



Example 1 Write $4\frac{5}{8}$ as an improper fraction.

$$\begin{aligned}
 4\frac{5}{8} &= 4 + \frac{5}{8} && \text{Definition of mixed number} \\
 &= \frac{32}{8} + \frac{5}{8} && \text{1 whole} = \frac{8}{8}. \text{ So, 4 wholes} = \frac{32}{8}. \\
 &= \frac{37}{8} && \text{Add.}
 \end{aligned}$$

► $4\frac{5}{8}$ written as an improper fraction is $\frac{37}{8}$.

Example 2 Write $\frac{19}{7}$ as a mixed number.

$$\begin{array}{r}
 2 \\
 7 \overline{)19} \\
 \underline{14} \\
 5
 \end{array}$$

Divide the numerator, 19, by the denominator, 7. The quotient is 2.

The remainder is 5. Write the remainder as a fraction, $\frac{\text{remainder}}{\text{divisor}}$.

► $\frac{19}{7}$ written as a mixed number is $2\frac{5}{7}$.

Practice

Check your answers at BigIdeasMath.com.

Write the mixed number as an improper fraction.

- | | | | |
|-------------------|--------------------|---------------------|---------------------|
| 1. $1\frac{4}{5}$ | 2. $3\frac{1}{6}$ | 3. $10\frac{7}{10}$ | 4. $2\frac{12}{13}$ |
| 5. $6\frac{5}{9}$ | 6. $4\frac{3}{20}$ | 7. $7\frac{6}{7}$ | 8. $25\frac{2}{3}$ |

Write the improper fraction as a mixed number.

- | | | | |
|---------------------|--------------------|--------------------|---------------------|
| 9. $\frac{9}{2}$ | 10. $\frac{13}{5}$ | 11. $\frac{25}{3}$ | 12. $\frac{31}{9}$ |
| 13. $\frac{59}{10}$ | 14. $\frac{43}{4}$ | 15. $\frac{35}{8}$ | 16. $\frac{67}{11}$ |

17. Find the improper fraction with a denominator of 8 that is equivalent to $3\frac{1}{2}$. $\frac{28}{8}$

18. Find the improper fraction with a denominator of 12 that is equivalent to $5\frac{3}{4}$. $\frac{69}{12}$