Key Concept and Vocabulary

Product of Powers Property

To multiply powers with the same base, add their exponents.

Numbers:
$$2^3 \cdot 2^4 = 2^{3+4} = 2^7$$

Algebra:
$$a^m \cdot a^n = a^{m+n}$$



Visual Model

$$2^{3} \cdot 2^{4} = (2 \cdot 2 \cdot 2) \cdot (2 \cdot 2 \cdot 2 \cdot 2)$$
$$= 2^{7}$$

$$(-4)^2 \cdot (-4)^3 = [(-4) \cdot (-4)][(-4) \cdot (-4) \cdot (-4)]$$

= $(-4)^5$

Skill Examples

1.
$$5^2 \cdot 5^5 = 5^{2+5} = 5^7$$

2.
$$(-3)^8 \cdot (-3)^2 = (-3)^{8+2} = (-3)^{10}$$

3.
$$(7^2)^3 = 7^2 \cdot 7^2 \cdot 7^2 = 7^{2+2+2} = 7^6$$

4.
$$(v^3)^4 = v^3 \cdot v^3 \cdot v^3 \cdot v^3 = v^{3+3+3+3} = v^{12}$$

5.
$$(3x)^3 = 3x \cdot 3x \cdot 3x$$
$$= (3 \cdot 3 \cdot 3) \cdot (x \cdot x \cdot x)$$
$$= 3^3 \cdot x^3$$
$$= 27x^3$$

Application Example

6. A gigabyte of computer storage space is 2³⁰ bytes. A computer has a total storage space of 128 gigabytes. How many bytes of total storage space does the computer have? Write your answer as a power.

Notice that 128 can be written as a power, 2^7 .

Total number _ Number of bytes _ Number of bytes in a gigabyte of gigabytes $=2^{30} \cdot 2^7$ $=2^{30+7}$ $= 2^{37}$

The computer has 2³⁷ bytes of total storage space.

Check your answers at BigIdeasMath.com. 😀

PRACTICE MAKES PURR-FECT®

Simplify the expression. Write your answer as a power.

7.
$$8^3 \cdot 8^6 =$$
 8. $3^4 \cdot 3^2 =$ **9.** $6^7 \cdot 6^5 =$

8.
$$3^4 \cdot 3^2 =$$

9.
$$6^7 \cdot 6^5 =$$

10.
$$(-5)^3 \cdot (-5)^7 =$$
 11. $(-10)^6 \cdot (-10)^2 =$ **12.** $(-2)^4 \cdot (-2)^5 =$

11.
$$(-10)^6 \cdot (-10)^2 =$$

12.
$$(-2)^4 \cdot (-2)^5 =$$

13.
$$(9^4)^3 =$$
 ______ **15.** $(12^3)^2 =$ _____

14.
$$(4^5)^3 =$$

15.
$$(12^3)^2 =$$

16.
$$(z^3)^3 =$$

17.
$$(n^5)^2 =$$

16.
$$(z^3)^3 =$$
 17. $(n^5)^2 =$ **18.** $(w^2)^4 =$

Simplify the expression.

19.
$$(9y)^2 =$$

19.
$$(9y)^2 =$$
 ______ **20.** $(3b)^4 =$ _____

21.
$$(2a)^5 =$$

22. ARTIFACT A display case for the artifact is in the shape of a cube. Each side of the display case is four times the side length of the artifact. Write and simplify an expression for the volume of the case.

