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Essential Question When a chord intersects a tangent line or another chord, what relationships exist among the angles and arcs formed?

## 1 EXPLORATION: Angles Formed by a Chord and Tangent Line

Go to BigIdeasMath.com for an interactive tool to investigate this exploration.
Work with a partner. Use dynamic geometry software. Sample
a. Construct a chord in a circle.

At one of the endpoints of the chord, construct a tangent line to the circle.
b. Find the measures of the two angles formed by the chord and the tangent line.

c. Find the measures of the two circular arcs determined by the chord.
d. Repeat parts (a)-(c) several times. Record your results in the following table. Then write a conjecture that summarizes the data.

| Angle <br> Measure 1 | Angle <br> Measure 2 | Circular Arc <br> Measure 1 | Circular Arc <br> Measure 2 |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

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### 10.5 Angle Relationships in Circles (continued)

## 2 EXPLORATION: Angles Formed by Intersecting Chords

## Go to BigIdeasMath.com for an interactive tool to investigate this exploration.

Work with a partner. Use dynamic geometry software.
Sample
a. Construct two chords that intersect inside a circle.
b. Find the measure of one of the angles formed by the intersecting chords.
c. Find the measures of the arcs intercepted by the angle in part (b) and its vertical angle. What do you observe?

d. Repeat parts (a)-(c) several times. Record your results in the following table. Then write a conjecture that summarizes the data.

| Angle Measure | Arc Measures | Observations |
| :--- | :--- | :--- |
|  |  |  |
|  |  |  |
|  |  |  |
|  |  |  |

## Communicate Your Answer

3. When a chord intersects a tangent line or another chord, what relationships exist among the angles and arcs formed?
4. Line $m$ is tangent to the circle in the figure at the right. Find the measure of $\angle 1$.

5. Two chords intersect inside a circle to form a pair of vertical angles with measures of $55^{\circ}$. Find the sum of the measures of the arcs intercepted by the two angles.
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## 10.5 <br> Notetaking with Vocabulary

In your own words, write the meaning of each vocabulary term.
circumscribed angle

## Theorems

## Theorem 10.14 Tangent and Intersected Chord Theorem

If a tangent and a chord intersect at a point on a circle, then the measure of each angle formed is one-half the measure of its intercepted arc.

$m \angle 1=\frac{1}{2} m \widehat{A B} \quad m \angle 2=\frac{1}{2} m \widehat{B C A}$

## Notes:

## Core Concepts

## Intersecting Lines and Circles

If two nonparallel lines intersect a circle, there are three places where the lines can intersect.

on the circle

inside the circle

outside the circle

Notes:

## Theorems

## Theorem 10.15 Angles Inside the Circle Theorem

If two chords intersect inside a circle, then the measure of each angle is one-half the sum of the measure of the arcs intercepted by the angle and its vertical angle.

## Notes:


$m \angle 1=\frac{1}{2}(m \overparen{D C}+m \overparen{A B})$,
$m \angle 2=\frac{1}{2}(m \overparen{A D}+m \overparen{B C})$
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### 10.5 Notetaking with Vocabulary (continued)

## Theorem 10.16 Angles Outside the Circle Theorem

If a tangent and a secant, two tangents, or two secants intersect outside a circle, then the measure of the angle formed is one-half the difference of the measures of the intercepted arcs.

$m \angle 1=\frac{1}{2}(m \overparen{B C}-m \overparen{A C})$
$m \angle 2=\frac{1}{2}(m \overparen{P Q R}-m \overparen{P R})$
$m \angle 3=\frac{1}{2}(m \overparen{X Y}-m \overparen{W Z})$

## Notes:

## Core Concepts

## Circumscribed Angle

A circumscribed angle is an angle whose sides are tangent to a circle.

Notes:


## Theorems

## Theorem 10.17 Circumscribed Angle Theorem

The measure of a circumscribed angle is equal to $180^{\circ}$ minus the measure of the central angle that intercepts the same arc.

## Notes:



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m \angle A D B=180^{\circ}-m \angle A C B
$$

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### 10.5 Notetaking with Vocabulary (continued)

## Extra Practice

In Exercises 1-3, $\overrightarrow{C D}$ is tangent to the circle. Find the indicated measure.

1. $m \angle A B C$
2. $m \overparen{A B}$
3. $m \overparen{A E B}$


In Exercises 4 and 5, $m \widehat{A D B}=220^{\circ}$ and $m \angle B=21^{\circ}$. Find the indicated measure.
4. $m \overparen{A B}$
5. $m \angle A C B$


## In Exercises 6-9, find the value of $\boldsymbol{x}$.

6. 


7.

8.

9.


