

10.3**Using Chords**

For use with Exploration 10.3

Essential Question What are two ways to determine when a chord is a diameter of a circle?

1 EXPLORATION: Drawing Diameters

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

Work with a partner. Use dynamic geometry software to construct a circle of radius 5 with center at the origin. Draw a diameter that has the given point as an endpoint. Explain how you know that the chord you drew is a diameter.

a. $(4, 3)$

b. $(0, 5)$

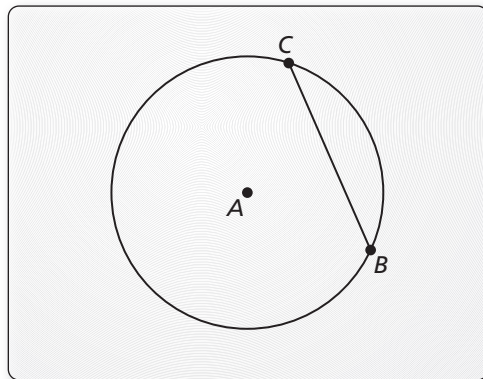
c. $(-3, 4)$

d. $(-5, 0)$

2 EXPLORATION: Writing a Conjecture about Chords

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

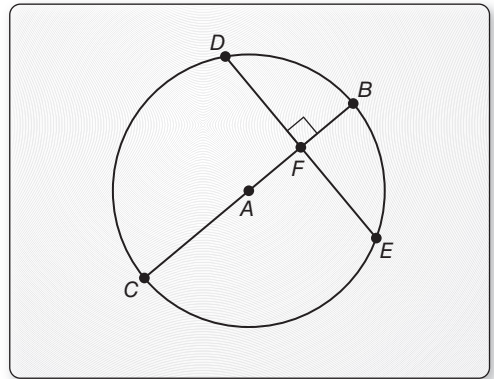
Work with a partner. Use dynamic geometry software to construct a chord \overline{BC} of a circle A . Construct a chord on the perpendicular bisector of \overline{BC} . What do you notice? Change the original chord and the circle several times. Are your results always the same? Use your results to write a conjecture.



10.3 Using Chords (continued)**3** **EXPLORATION:** A Chord Perpendicular to a Diameter

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

Work with a partner. Use dynamic geometry software to construct a diameter \overline{BC} of a circle A . Then construct a chord \overline{DE} perpendicular to \overline{BC} at point F . Find the lengths DF and EF . What do you notice? Change the chord perpendicular to \overline{BC} and the circle several times. Do you always get the same results? Write a conjecture about a chord that is perpendicular to a diameter of a circle.

**Communicate Your Answer**

4. What are two ways to determine when a chord is a diameter of a circle?

10.3**Notetaking with Vocabulary**

For use after Lesson 10.3

In your own words, write the meaning of each vocabulary term.

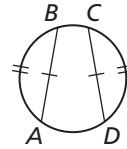
chord

arc

diameter

Theorems**Theorem 10.6 Congruent Corresponding Chords Theorem**

In the same circle, or in congruent circles, two minor arcs are congruent if and only if their corresponding chords are congruent.

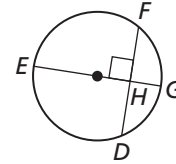
Notes:

$$\widehat{AB} \cong \widehat{CD} \text{ if and only if } \overline{AB} \cong \overline{CD}.$$

10.3 Notetaking with Vocabulary (continued)

Theorem 10.7 Perpendicular Chord Bisector Theorem

If a diameter of a circle is perpendicular to a chord, then the diameter bisects the chord and its arc.

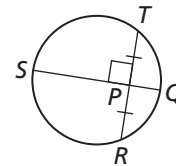


If \overline{EG} is a diameter and $\overline{EG} \perp \overline{DF}$,
then $\overline{HD} \cong \overline{HF}$ and $\widehat{GD} \cong \widehat{GF}$.

Notes:

Theorem 10.8 Perpendicular Chord Bisector Converse

If one chord of a circle is a perpendicular bisector of another chord, then the first chord is a diameter.

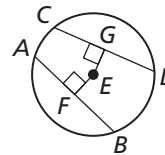


If \overline{QS} is a perpendicular bisector of \overline{TR} ,
then \overline{QS} is a diameter of the circle.

Notes:

Theorem 10.9 Equidistant Chords Theorem

In the same circle, or in congruent circles, two chords are congruent if and only if they are equidistant from the center.



$\overline{AB} \cong \overline{CD}$ if and only if $EF = EG$.

Notes:

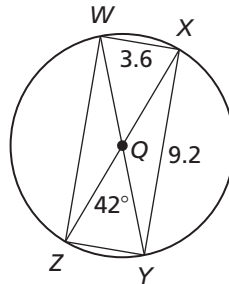
10.3 Notetaking with Vocabulary (continued)

Extra Practice

In Exercises 1–4, find the measure of the arc or chord in $\odot Q$.

1. $m\widehat{WX}$

2. YZ

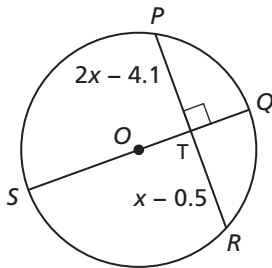


3. WZ

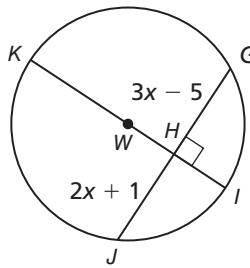
4. $m\widehat{XY}$

In Exercises 5 and 6, find the value of x .

5.

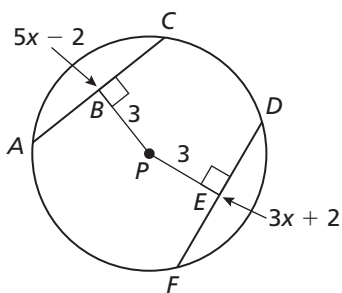


6.



In Exercises 7 and 8, find the radius of the circle.

7.



8.

