

# 3.5

## Equations of Parallel and Perpendicular Lines

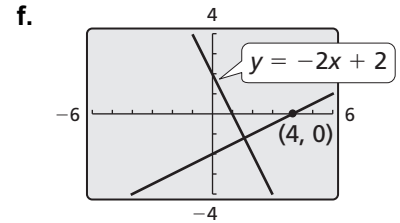
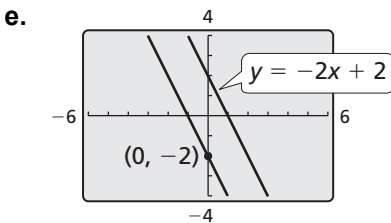
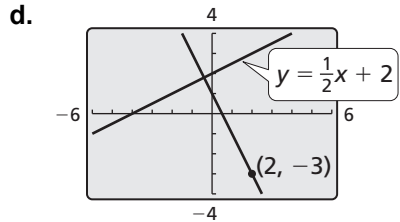
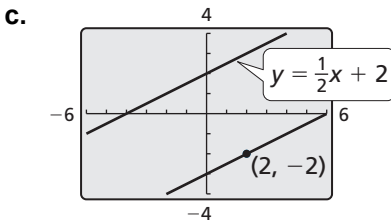
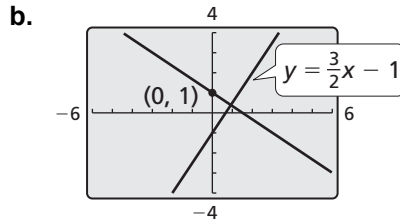
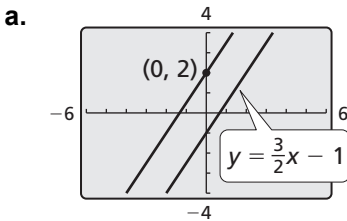
For use with Exploration 3.5

**Essential Question** How can you write an equation of a line that is parallel or perpendicular to a given line and passes through a given point?

### 1 EXPLORATION: Writing Equations of Parallel and Perpendicular Lines

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

**Work with a partner.** Write an equation of the line that is parallel or perpendicular to the given line and passes through the given point. Use a graphing calculator to verify your answer. What is the relationship between the slopes?

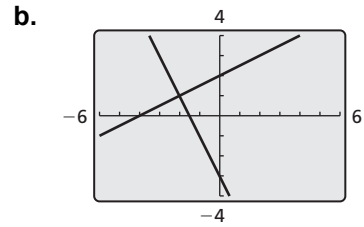
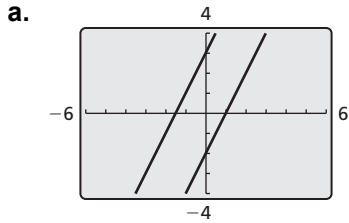


**3.5 Equations of Parallel and Perpendicular Lines (continued)**

**2 EXPLORATION:** Writing Equations of Parallel and Perpendicular Lines

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

**Work with a partner.** Write the equations of the parallel or perpendicular lines. Use a graphing calculator to verify your answers.



**Communicate Your Answer**

3. How can you write an equation of a line that is parallel or perpendicular to a given line and passes through a given point?
  
4. Write an equation of the line that is (a) parallel and (b) perpendicular to the line  $y = 3x + 2$  and passes through the point  $(1, -2)$ .

**3.5****Notetaking with Vocabulary**

For use after Lesson 3.5

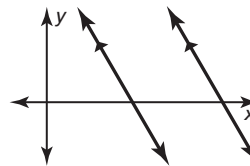
In your own words, write the meaning of each vocabulary term.

directed line segment

**Theorems****Theorem 3.13 Slopes of Parallel Lines**

In a coordinate plane, two nonvertical lines are parallel if and only if they have the same slope.

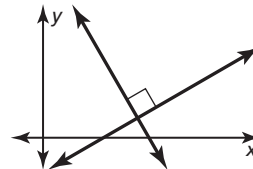
Any two vertical lines are parallel.

**Notes:**

$$m_1 = m_2$$

**Theorem 3.14 Slopes of Perpendicular Lines**In a coordinate plane, two nonvertical lines are perpendicular if and only if the product of their slopes is  $-1$ .

Horizontal lines are perpendicular to vertical lines.

**Notes:**

$$m_1 \cdot m_2 = -1$$

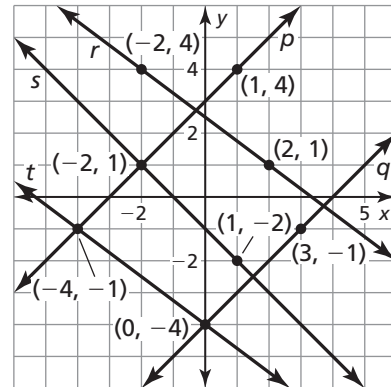
**3.5** Notetaking with Vocabulary (continued)

**Extra Practice**

In Exercises 1 and 2, find the coordinates of point  $P$  along the directed line segment  $AB$  so that  $AP$  to  $PB$  is the given ratio.

1.  $A(-2, 7), B(-4, 1)$ ; 3 to 1                      2.  $A(3, 1), B(8, -2)$ ; 2 to 3

3. Determine which of the lines are parallel and which of the lines are perpendicular.



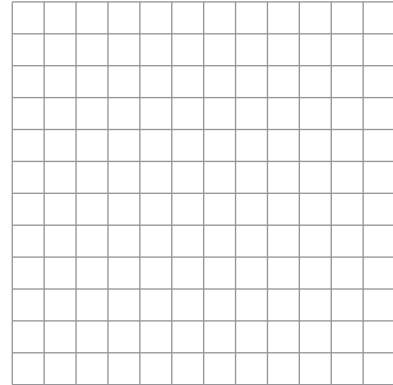
4. Tell whether the lines through the given points are *parallel*, *perpendicular*, or *neither*. Justify your answer.

Line 1:  $(2, 0), (-2, 2)$

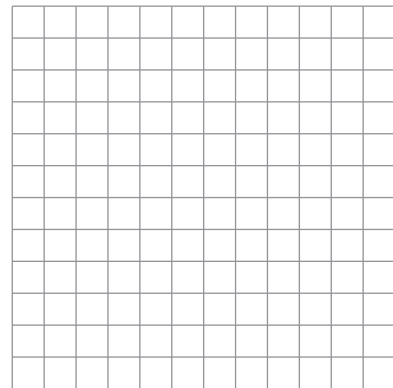
Line 2:  $(1, -2), (4, 4)$

**3.5** Notetaking with Vocabulary (continued)

5. Write an equation of the line passing through point  $P(3, -2)$  that is parallel to  $y = \frac{2}{3}x - 1$ . Graph the equations of the lines to check that they are parallel.



6. Write an equation of the line passing through point  $P(-2, 2)$  that is perpendicular to  $y = 2x + 3$ . Graph the equations of the lines to check that they are perpendicular.



7. Find the distance from point  $A(0, 5)$  to  $y = -3x - 5$ .