

# 7.7

## Factoring Special Products

For use with Exploration 7.7

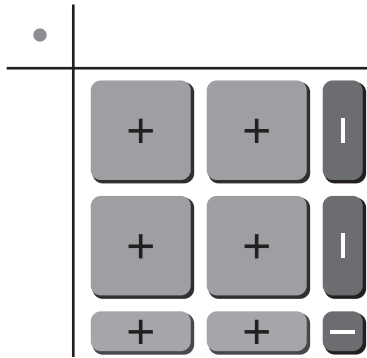
**Essential Question** How can you recognize and factor special products?

### 1 EXPLORATION: Factoring Special Products

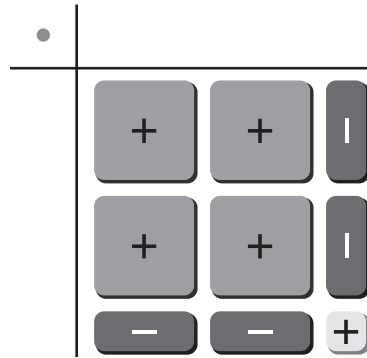
Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

**Work with a partner.** Use algebra tiles to write each polynomial as the product of two binomials. Check your answer by multiplying. State whether the product is a “special product” that you studied in Section 7.3.

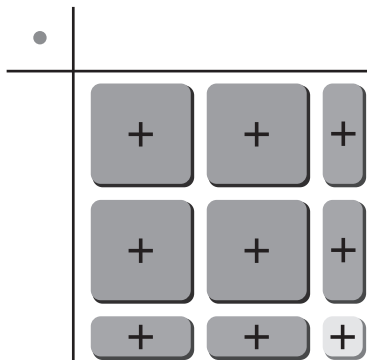
a.  $4x^2 - 1 =$  \_\_\_\_\_



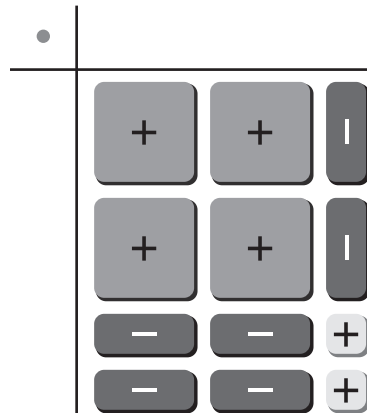
b.  $4x^2 - 4x + 1 =$  \_\_\_\_\_



c.  $4x^2 + 4x + 1 =$  \_\_\_\_\_



d.  $4x^2 - 6x + 2 =$  \_\_\_\_\_

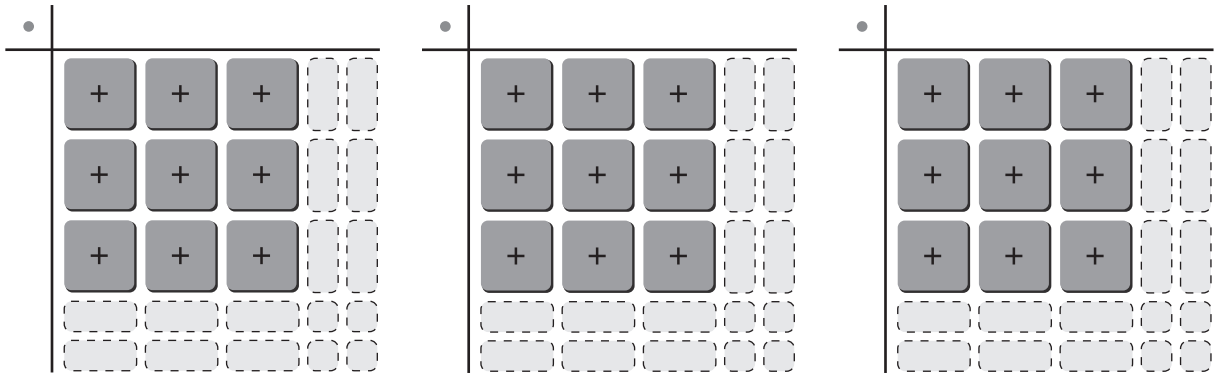


**7.7 Factoring Special Products (continued)**

**2 EXPLORATION: Factoring Special Products**

Go to *BigIdeasMath.com* for an interactive tool to investigate this exploration.

**Work with a partner.** Use algebra tiles to complete the rectangular arrays in three different ways, so that each way represents a different special product. Write each special product in standard form and in factored form.



**Communicate Your Answer**

3. How can you recognize and factor special products? Describe a strategy for recognizing which polynomials can be factored as special products.

4. Use the strategy you described in Question 3 to factor each polynomial.

a.  $25x^2 + 10x + 1$

b.  $25x^2 - 10x + 1$

c.  $25x^2 - 1$

**7.7****Notetaking with Vocabulary**

For use after Lesson 7.7

In your own words, write the meaning of each vocabulary term.

polynomial

trinomial

**Core Concepts****Difference of Two Squares Pattern****Algebra**

$$a^2 - b^2 = (a + b)(a - b)$$

**Example**

$$x^2 - 9 = x^2 - 3^2 = (x + 3)(x - 3)$$

**Notes:****Perfect Square Trinomial Pattern****Algebra**

$$a^2 + 2ab + b^2 = (a + b)^2$$

**Example**

$$\begin{aligned}x^2 + 6x + 9 &= x^2 + 2(x)(3) + 3^2 \\ &= (x + 3)^2\end{aligned}$$

$$a^2 - 2ab + b^2 = (a - b)^2$$

$$\begin{aligned}x^2 - 6x + 9 &= x^2 - 2(x)(3) + 3^2 \\ &= (x - 3)^2\end{aligned}$$

**Notes:**

**7.7** Notetaking with Vocabulary (continued)**Extra Practice**

In Exercises 1–6, factor the polynomial.

1.  $s^2 - 49$

2.  $t^2 - 81$

3.  $16 - x^2$

4.  $4g^2 - 25$

5.  $36h^2 - 121$

6.  $81 - 49k^2$

In Exercises 7–12, use a special product pattern to evaluate the expression.

7.  $57^2 - 53^2$

8.  $38^2 - 32^2$

9.  $68^2 - 64^2$

10.  $45^2 - 40^2$

11.  $79^2 - 71^2$

12.  $86^2 - 84^2$

**7.7** Notetaking with Vocabulary (continued)

In Exercises 13–18, factor the polynomial.

13.  $x^2 + 16x + 64$

14.  $p^2 + 28p + 196$

15.  $r^2 - 26r + 169$

16.  $a^2 - 18a + 81$

17.  $36c^2 + 84c + 49$

18.  $100x^2 - 20x + 1$

In Exercises 19–24, solve the equation.

19.  $x^2 - 144 = 0$

20.  $9y^2 = 49$

21.  $c^2 + 14c + 49 = 0$

22.  $d^2 - 4d + 4 = 0$

23.  $n^2 + \frac{2}{3}n = -\frac{1}{9}$

24.  $-\frac{6}{5}k + \frac{9}{25} = -k^2$

25. The dimensions of a rectangular prism are  $(x + 1)$  feet by  $(x + 2)$  feet by 4 feet. The volume of the prism is  $(24x - 1)$  cubic feet. What is the value of  $x$ ?