# 8 Volume and Similar Solids

- 8.1 Volumes of Cylinders
- 8.2 Volumes of Cones
- 8.3 Volumes of Spheres
- 8.4 Surface Areas and Volumes of Similar Solids



"Dear Sir: Why do you sell dog food in tall cans and sell cat food in short cans?"



"Neither of these shapes is the optimal use of surface area when compared to volume."



"Do you know why the volume of a cone is one-third the volume of a cylinder with the same height and base?"

# What You Learned Before

### Finding the Area of a Composite Figure (7.G.6)

**Example 1** Find the area of the figure.





### Try It Yourself

Find the area of the figure.





### Finding the Areas of Circles (7.G.4)

 $\approx \frac{22}{7} \cdot 7^2$ 

 $=\frac{22}{7} \cdot 49$ 

 $= 154 \text{ mm}^2$ 

 $A = \pi r^2$ 

Example 2 F

7 mm

Find the area of the circle. Example 3 Fi

Find the area of the circle.



### Try It Yourself

Find the area of the circle.



# Essential Question How can you find the volume of a cylinder?

### **ACTIVITY:** Finding a Formula Experimentally

#### Work with a partner.

- **a.** Find the area of the face of a coin.
- **b.** Find the volume of a stack of a dozen coins.
- c. Write a formula for the volume of a cylinder.





### ACTIVITY: Making a Business Plan



#### Geometry

- In this lesson, you will
- find the volumes of cylinders.
  find the heights of adjuster arises the
- cylinders given the volumes.solve real-life problems.

Learning Standard 8.G.9 Work with a partner. You are planning to make and sell three different sizes of cylindrical candles. You buy 1 cubic foot of candle wax for \$20 to make 8 candles of each size.

- **a.** Design the candles. What are the dimensions of each size of candle?
- **b.** You want to make a profit of \$100. Decide on a price for each size of candle.
- **c.** Did you set the prices so that they are proportional to the volume of each size of candle? Why or why not?

2

### ACTIVITY: Science Experiment

Work with a partner. Use the diagram to describe how you can find the volume of a small object.





Consider Similar Problems How can you use the results of Activity 1 to find the volumes of the cylinders?

### **4 ACTIVITY:** Comparing Cylinders

#### Work with a partner.

- **a.** Just by looking at the two cylinders, which one do you think has the greater volume? Explain your reasoning.
- **b.** Find the volume of each cylinder. Was your prediction in part (a) correct? Explain your reasoning.





### -What Is Your Answer?

- 5. IN YOUR OWN WORDS How can you find the volume of a cylinder?
- **6.** Compare your formula for the volume of a cylinder with the formula for the volume of a prism. How are they the same?







"Base times tall, will fill 'em all."



Use what you learned about the volumes of cylinders to complete Exercises 3–5 on page 338.



### 3 Real-Life Application



So, about 471 cubic centimeters of salsa are missing from the jar.

#### EXAMPLE

Д

EXAMPLE

### Real-Life Application



About how many gallons of water does the watercooler bottle contain? (1 ft<sup>3</sup>  $\approx$  7.5 gal)

(A) 5.3 gallons (B) 10 gallons (C) 17 gallons (D) 40 gallons

Find the volume of the cylinder. The diameter is 1 foot. So, the radius is 0.5 foot.

V = Bh	Write formula for volume.
$=\pi(0.5)^2(1.7)$	Substitute.
$= 0.425 \pi \approx 1.3352$	Use a calculator.

So, the bottle contains about 1.3352 cubic feet of water. To find the number of gallons it contains, multiply by the conversion factor  $\frac{7.5 \text{ gal}}{1 \text{ ft}^3}$ .

1.3352 
$$\operatorname{ft}^{\mathfrak{F}} \times \frac{7.5 \text{ gal}}{1 \operatorname{ft}^{\mathfrak{F}}} \approx 10 \text{ gal}$$

The watercooler bottle contains about 10 gallons of water. So, the correct answer is **B**.

### On Your Own

- **3. WHAT IF?** In Example 3, the height of the salsa in the jar is 5 centimeters. How much salsa is missing from the jar?
- 4. A cylindrical water tower has a diameter of 15 meters and a height of 5 meters. About how many gallons of water can the tower contain? (1  $m^3 \approx 264$  gal)



### 8.1 Exercises





### Practice and Problem Solving

Find the volume of the cylinder. Round your answer to the nearest tenth.



**12. SWIMMING POOL** A cylindrical swimming pool has a diameter of 16 feet and a height of 4 feet. About how many gallons of water can the pool contain? Round your answer to the nearest whole number. (1  $\text{ft}^3 \approx 7.5 \text{ gal}$ )

#### Find the missing dimension of the cylinder. Round your answer to the nearest whole number.

**2 13.** Volume =  $250 \text{ ft}^3$ 







**16. CRITICAL THINKING** How does the volume of a cylinder change when its diameter is halved? Explain.

32 in.



**17. MODELING** A traditional "square" bale of hay is actually in the shape of a rectangular prism. Its dimensions are 2 feet by 2 feet by 4 feet. How many square bales contain the same amount of hay as one large "round" bale?

**18. ROAD ROLLER** A tank on a road roller is filled with water to make the roller heavy. The tank is a cylinder

that has a height of 6 feet and a radius of 2 feet. One cubic foot of water weighs 62.5 pounds. Find the weight of the water in the tank.

Round hay bale

- **19. VOLUME** A cylinder has a surface area of 1850 square meters and a radius of 9 meters. Estimate the volume of the cylinder to the nearest whole number.
- Water flows at 2 feet per second through a pipe with a diameter of 8 inches. 20. A cylindrical tank with a diameter of 15 feet and a height of 6 feet collects the water.
  - **a.** What is the volume, in cubic inches, of water flowing out of the pipe every second?
  - **b.** What is the height, in inches, of the water in the tank after 5 minutes?
  - c. How many minutes will it take to fill 75% of the tank?

#### Fair Game Review What you learned in previous grades & lessons Tell whether the triangle with the given side lengths is a right triangle. (Section 7.5) **21.** 20 m, 21 m, 29 m **22.** 1 in., 2.4 in., 2.6 in. **23.** 5.6 ft, 8 ft, 10.6 ft 24. MULTIPLE CHOICE Which ordered pair is the solution of the linear system 3x + 4y = -10 and 2x - 4y = 0? (Section 5.3) (A) (-6, 2) **(B)** (2, −6) $(\mathbf{C})$ (-2, -1) $(\mathbf{D})$ (-1, -2)

# 8.2 Volumes of Cones

# Essential Question How can you find the volume of a cone?

You already know how the volume of a pyramid relates to the volume of a prism. In this activity, you will discover how the volume of a cone relates to the volume of a cylinder.



### (1

### **ACTIVITY:** Finding a Formula Experimentally

#### Work with a partner. Use a paper cup that is shaped like a cone.

- Estimate the height of the cup.
- Trace the top of the cup on a piece of paper. Find the diameter of the circle.
- Use these measurements to draw a net for a cylinder with the same base and height as the paper cup.
- Cut out the net. Then fold and tape it to form an open cylinder.
- Fill the paper cup with rice. Then pour the rice into the cylinder. Repeat this until the cylinder is full. How many cones does it take to fill the cylinder?
- Use your result to write a formula for the volume of a cone.



In this lesson, you will

given the volumes.solve real-life problems.Learning Standard

find the volumes of cones.find the heights of cones

Geometry

8.G.9

#### **ACTIVITY:** Summarizing Volume Formulas

Work with a partner. You can remember the volume formulas for prisms, cylinders, pyramids, and cones with just two concepts.

#### Volumes of Prisms and Cylinders

- Volume = Area of base  $\times$

#### Volumes of Pyramids and Cones

Volume =

Volume of prism or cylinder with same base and height

Make a list of all the formulas you need to remember to find the area of a base. Talk about strategies for remembering these formulas.

2

### **3** ACTIVITY: Volumes of Oblique Solids

Work with a partner. Think of a stack of paper. When you adjust the stack so that the sides are oblique (slanted), do you change the volume of the stack? If the volume of the stack does not change, then the formulas for volumes of right solids also apply to oblique solids.



### 8.2 Lesson





### Volume of a Cone

Words



The *height* of a cone is the perpendicular distance from the base to the vertex.



The volume *V* of a cone is one-third the product of the area of the base



### **EXAMPLE The Finding the Volume of a Cone**







Write formula for volume.

Use a calculator.

Substitute.



• The volume is about 25.1 cubic meters.

### **EXAMPLE** 2 Finding the Height of a Cone

Find the height of the cone. Round your answer to the nearest tenth.



• The height is about 11.3 feet.





Find the volume V or height h of the cone. Round your answer to the nearest tenth.



3 **Real-Life Application** EXAMPLE



You must answer a trivia question before the sand in the timer falls to the bottom. The sand falls at a rate of 50 cubic millimeters per second. How much time do you have to answer the question?

Use the formula for the volume of a cone to find the volume of the sand in the timer.

$$V = \frac{1}{3}Bh$$
 Write for  
$$= \frac{1}{3}\pi(10)^2(24)$$
 Substitut

ormula for volume.

ite.

 $= 800 \pi \approx 2513$ 

Use a calculator.

The volume of the sand is about 2513 cubic millimeters. To find the amount of time you have to answer the question, multiply the volume by the rate at which the sand falls.

$$2513 \text{ mm}^3 \times \frac{1 \text{ sec}}{50 \text{ mm}^3} = 50.26 \text{ sec}$$

So, you have about 50 seconds to answer the question. 

### On Your Own

- 3. WHAT IF? The sand falls at a rate of 60 cubic millimeters per second. How much time do you have to answer the question?
- 4. WHAT IF? The height of the sand in the timer is 12 millimeters, and the radius is 5 millimeters. How much time do you have to answer the question?

# 8.2 Exercises





- **1. VOCABULARY** Describe the height of a cone.
- **2. WRITING** Compare and contrast the formulas for the volume of a pyramid and the volume of a cone.
- **3. REASONING** You know the volume of a cylinder. How can you find the volume of a cone with the same base and height?

# Practice and Problem Solving

Find the volume of the cone. Round your answer to the nearest tenth.



#### Find the missing dimension of the cone. Round your answer to the nearest tenth.



**22.** In Example 3, you use a different timer with the same dimensions. The sand in this timer has a height of 30 millimeters. How much time do you have to answer the question?

### Fair Game Review What you learned in previous grades & lessons

The vertices of a figure are given. Rotate the figure as described. Find the coordinates of the image. (Section 2.4)

- **23.** *A*(-1, 1), *B*(2, 3), *C*(2, 1) 90° counterclockwise about vertex *A*
- **24.** E(-4, 1), F(-3, 3), G(-2, 3), H(-1, 1)180° about the origin
- **25. MULTIPLE CHOICE**  $\triangle ABC \sim \triangle XYZ$  by a scale factor of 3. How many times greater is the area of  $\triangle XYZ$  than the area of  $\triangle ABC$ ? (*Section 2.6*)
  - **(A)**  $\frac{1}{9}$  **(B)**  $\frac{1}{3}$
  - **(C)** 3 **(D)** 9

A = C

# 8 Study Help

You can use a **formula triangle** to arrange variables and operations of a formula. Here is an example of a formula triangle for the volume of a cylinder.

To find an unknown variable, use the other variables and the operation between them. For example, to find the area B of the base, cover up the B. Then you can see that you divide the volume V by the height h.



### On Your Own

Make a formula triangle to help you study this topic. (*Hint:* Your formula triangle may have a different form than what is shown in the example.)

**1.** volume of a cone

After you complete this chapter, make formula triangles for the following topics.

- 2. volume of a sphere
- 3. volume of a composite solid
- 4. surface areas of similar solids
- 5. volumes of similar solids



"See how a formula triangle works? Cover any variable and you get its formula."



Find the missing dimension of the solid. Round your answer to the nearest tenth. *(Section 8.1 and Section 8.2)* 





**7. PAPER CONE** The paper cone can hold 84.78 cubic centimeters of water. What is the height of the cone? (*Section 8.2*)

8. **GEOMETRY** Triple both dimensions of the cylinder. How many times greater is the volume of the new cylinder than the volume of the original cylinder? *(Section 8.1)* 







# 8.3 Volumes of Spheres

# Essential Question How can you find the volume of a sphere?

A **sphere** is the set of all points in space that are the same distance from a point called the *center*. The *radius r* is the distance from the center to any point on the sphere.

A sphere is different from the other solids you have studied so far because it does not have a base. To discover the volume of a sphere, you can use an activity similar to the one in the previous section.



### **ACTIVITY:** Exploring the Volume of a Sphere

Work with a partner. Use a plastic ball similar to the one shown.

- Estimate the diameter and the radius of the ball.
- Use these measurements to draw a net for a cylinder with a diameter and a height equal to the diameter of the ball. How is the height *h* of the cylinder related to the radius *r* of the ball? Explain.
- Cut out the net. Then fold and tape it to form an open cylinder. Make two marks on the cylinder that divide it into thirds, as shown.
  - Cover the ball with aluminum foil or tape. Leave one hole open. Fill the ball with rice. Then pour the rice into the cylinder. What fraction of the cylinder is filled with rice?









Geometry

In this lesson, you will

- find the volumes of spheres.find the radii of spheres
- given the volumes.solve real-life problems.

Learning Standard 8.G.9

### **2 ACTIVITY:** Deriving the Formula for the Volume of a Sphere



# Work with a partner. Use the results from Activity 1 and the formula for the volume of a cylinder to complete the steps.



### **ACTIVITY:** Deriving the Formula for the Volume of a Sphere

Work with a partner. Imagine filling the inside of a sphere with *n* small pyramids. The vertex of each pyramid is at the center of the sphere. The height of each pyramid is approximately equal to *r*, as shown. Complete the steps. (The surface area of a sphere is equal to  $4\pi r^2$ .)



Show how this result is equal to the result in Activity 2.

area of base, B

3

### What Is Your Answer?

- **4. IN YOUR OWN WORDS** How can you find the volume of a sphere?
- **5.** Describe the intersection of the plane and the sphere. Then explain how to find the volume of each section of the solid.





Use what you learned about the volumes of spheres to complete Exercises 3–5 on page 352.



EXAMPLE

1

### Finding the Volume of a Sphere

Find the volume of the sphere. Round your answer to the nearest tenth.

Substitute 4 for r.

Use a calculator.

Simplify.

Write formula for volume.



$V = \frac{4}{3} \pi r^3$	
$=\frac{4}{3}\pi(4)^3$	
$=rac{256}{3}\pi$	
$\approx 268.1$	

The volume is about 268.1 cubic centimeters.



Multi-Language Glossary at BigIdeasMath com

### On Your Own



Find the volume V or radius r of the sphere. Round your answer to the nearest tenth, if necessary.



#### EXAMPLE

### 3 Finding the Volume of a Composite Solid



Study Tip

In Example 3, the

height of the cylindrical

part of the silo is the difference of the silo

height and the radius of the hemisphere. 52 - 12 = 40 ft A <mark>hemisphere</mark> is one-half of a sphere. The top of the silo is a hemisphere with a radius of 12 feet. What is the volume of the silo? Round your answer to the nearest thousand.

The silo is made up of a cylinder and a hemisphere. Find the volume of each solid.



So, the volume is  $5760\pi + 1152\pi = 6912\pi \approx 22,000$  cubic feet.



### On Your Own

Find the volume of the composite solid. Round your answer to the nearest tenth.





# 8.3 Exercises



## Vocabulary and Concept Check

- 1. VOCABULARY How is a sphere different from a hemisphere?
- **2.** WHICH ONE DOESN'T BELONG? Which figure does *not* belong with the other three? Explain your reasoning.





Find the volume of the sphere. Round your answer to the nearest tenth.



Find the radius of the sphere with the given volume.

**9.** Volume =  $972 \pi \, \text{mm}^3$ 

2

- **10.** Volume =  $4.5 \pi \, \text{cm}^3$
- **11.** Volume =  $121.5 \pi \text{ ft}^3$



- **12. GLOBE** The globe of the Moon has a radius of 10 inches. Find the volume of the globe. Round your answer to the nearest whole number.
- **13. SOFTBALL** A softball has a volume of  $\frac{125}{6}\pi$  cubic inches. Find the radius of the softball.

Find the volume of the composite solid. Round your answer to the nearest tenth.



- **17. REASONING** A sphere and a right cylinder have the same radius and volume. Find the radius *r* in terms of the height *h* of the cylinder.
- **18. PACKAGING** A cylindrical container of three rubber balls has a height of 18 centimeters and a diameter of 6 centimeters. Each ball in the container has a radius of 3 centimeters. Find the amount of space in the container that is not occupied by rubber balls. Round your answer to the nearest whole number.





- **19. BASKETBALL** The basketball shown is packaged in a box that is in the shape of a cube. The edge length of the box is equal to the diameter of the basketball. What is the surface area and the volume of the box?
- **20.** Your friend says that the volume of a sphere with radius *r* is four times the volume of a cone with radius *r*. When is this true? Justify your answer.



**Essential Question** When the dimensions of a solid increase by a factor of *k*, how does the surface area change? How does the volume change?



Work with a partner. Copy and complete the table. Describe the pattern. Are the dimensions proportional? Explain your reasoning.

Radius	1	1	1	1	1
Height	1	2	3	4	5
Surface Area					
Volume					



Radius	1	2	3	4	5
Height	1	2	3	4	5
Surface Area					
Volume					

Geometry

- In this lesson, you will
- identify similar solids.
   use properties of similar solids to find missing measures.
- understand the relationship between surface areas of similar solids.
- understand the relationship between volumes of similar solids.
- solve real-life problems.

Applying Standard 8.G.9 a.

b.

### **2 ACTIVITY:** Comparing Surface Areas and Volumes

Work with a partner. Copy and complete the table. Describe the pattern. Are the dimensions proportional? Explain.



Base Side	6	12	18	24	30
Height	4	8	12	16	20
Slant Height	5	10	15	20	25
Surface Area					
Volume					

### -What Is Your Answer?

- **3. IN YOUR OWN WORDS** When the dimensions of a solid increase by a factor of *k*, how does the surface area change?
- **4. IN YOUR OWN WORDS** When the dimensions of a solid increase by a factor of *k*, how does the volume change?
- **5. REPEATED REASONING** All the dimensions of a prism increase by a factor of 5.
  - a. How many times greater is the surface area? Explain.





Use what you learned about surface areas and volumes of similar solids to complete Exercise 3 on page 359.

### 8.4 Lesson



Cylinder A

6 m

Not proportional

4 m



Similar solids are solids that have the same shape and proportional corresponding dimensions.

### EXAMPLE

5 m

3 m

1





**Identifying Similar Solids** 

Check to see if corresponding dimensions are proportional.

#### Cylinder A and Cylinder B

Cylinder C



Cone X

13 vd

<u>Height of A <math>=</math> 4</u>	Radius of A $= 6$
Height of B $\overline{3}$	Radius of B 5

Cylinder A and Cylinder C

 $\frac{\text{Height of A}}{\text{Height of C}} = \frac{4}{5} \qquad \qquad \frac{\text{Radius of A}}{\text{Radius of C}} = \frac{6}{7.5} = \frac{4}{5} \qquad \qquad \text{Proportional}$ 

So, Cylinder C is similar to Cylinder A.

### **EXAMPLE 2** Finding Missing Measures in Similar Solids

### The cones are similar. Find the missing slant height $\ell$ .



• The slant height is 18.2 yards.

### On Your Own

- 1. Cylinder D has a radius of 7.5 meters and a height of 4.5 meters. Which cylinder in Example 1 is similar to Cylinder D?
- **2.** The prisms at the right are similar. Find the missing width and length.



low You're Ready

Exercises 4–9



**Linear Measures** 



Solid A

Solid B

#### **Surface Areas of Similar Solids**

When two solids are similar, the ratio of their surface areas is equal to the square of the ratio of their corresponding linear measures.



### **3** Finding Surface Area

**EXAMPLE** 



### On Your Own

The solids are similar. Find the surface area of the red solid. Round your answer to the nearest tenth.





#### **Volumes of Similar Solids**

When two solids are similar, the ratio of their volumes is equal to the cube of the ratio of their corresponding linear measures.



4 in.

 $\frac{\text{Volume of A}}{\text{Volume of B}} = \left(\frac{a}{b}\right)^3$ 



### E 4 Finding Volume



Volume =  $2000 \text{ ft}^3$ 

Study Tip 🦯
When the dimensions
of a solid are multiplied
by k, the surface area
is multiplied by $k^2$ and
the volume is multiplied
by $k^3$ .

### The dimensions of the touch tank at an aquarium are doubled. What is the volume of the new touch tank?

A	150 ft <sup>3</sup>	B	4000 ft <sup>3</sup>
<b>C</b>	8000 ft <sup>3</sup>	D	16,000 ft <sup>3</sup>

The dimensions are doubled, so the ratio of the dimensions of the original tank to the dimensions of the new tank is 1:2.

$$\frac{\text{Original volume}}{\text{New volume}} = \left(\frac{\text{Original dimension}}{\text{New dimension}}\right)^3$$
$$\frac{2000}{V} = \left(\frac{1}{2}\right)^3 \qquad \text{Substitute.}$$
$$\frac{2000}{V} = \frac{1}{8} \qquad \text{Evaluate.}$$
$$16,000 = V \qquad \text{Cross Products Property}$$

The volume of the new tank is 16,000 cubic feet. So, the correct answer is **D**.

### On Your Own

Now You're Ready Exercises 10–13 The solids are similar. Find the volume of the red solid. Round your answer to the nearest tenth.





### Vocabulary and Concept Check

- 1. VOCABULARY What are similar solids?
- **2. OPEN-ENDED** Draw two similar solids and label their corresponding linear measures.

# Practice and Problem Solving

- **3.** NUMBER SENSE All the dimensions of a cube increase by a factor of  $\frac{3}{2}$ .
  - a. How many times greater is the surface area? Explain.
  - b. How many times greater is the volume? Explain.



#### The solids are similar. Find the missing dimension(s).



The solids are similar. Find the surface area *S* or volume *V* of the red solid. Round your answer to the nearest tenth.



- **14. ERROR ANALYSIS** The ratio of the corresponding linear measures of two similar solids is 3:5. The volume of the smaller solid is 108 cubic inches. Describe and correct the error in finding the volume of the larger solid.
- **15. MIXED FRUIT** The ratio of the corresponding linear measures of two similar cans of fruit is 4 to 7. The smaller can has a surface area of 220 square centimeters. Find the surface area of the larger can.



The volume of the larger solid is 300 cubic inches.

**16. ENGINE** The volume of a car engine is 390 cubic inches. Which scale model of the car has the greater engine volume, a 1 : 18 scale model or a 1 : 24 scale model? How much greater is it?



- **17. MARBLE STATUE** You have a small marble statue of Wolfgang Mozart. It is 10 inches tall and weighs 16 pounds. The original statue is 7 feet tall.
  - **a.** Estimate the weight of the original statue. Explain your reasoning.
  - **b.** If the original statue were 20 feet tall, how much would it weigh?
- **18. REPEATED REASONING** The largest doll is 7 inches tall. Each of the other dolls is 1 inch shorter than the next

larger doll. Make a table that compares the surface areas and the volumes of the seven dolls.





Wolfgang Mozart

**19.** Precision: You and a friend make paper cones to collect beach glass. You cut out the largest possible three-fourths circle from each piece of paper.



- **a.** Are the cones similar? Explain your reasoning.
  - Your friend says that because your sheet of paper is twice as large, your cone will hold exactly twice the volume of beach glass. Is this true? Explain your reasoning.



### Fair Game Review What you learned in previous grades & lessons

Draw the figure and its reflection in the *x*-axis. Identify the coordinates of the image. (Section 2.3)

**20.** A(1, 1), B(3, 4), C(4, 2) **21.** J(-3, 0), K(-4, 3), L(-1, 4)

**22. MULTIPLE CHOICE** Which system of linear equations has no solution? *(Section 5.4)* 

(A) y = 4x + 1 y = -4x + 1 y = 2x + 7(B) y = 2x - 7 y = 2x + 7(C) 3x + y = 1 6x + 2y = 2x + 5y = 15

### 8.3–8.4 Quiz



Find the volume of the sphere. Round your answer to the nearest tenth. (Section 8.3)

2.





### Find the radius of the sphere with the given volume. (Section 8.3)

- **3.** Volume =  $4500 \pi \text{ yd}^3$
- **5.** Find the volume of the composite solid. Round your answer to the nearest tenth. *(Section 8.3)*



- **7.** The prisms are similar. Find the missing width and height. *(Section 8.4)* 
  - 10 in.





similar. (Section 8.4)

**4.** Volume =  $\frac{32}{2}\pi$  ft<sup>3</sup>



**6.** Determine whether the solids are

**8.** The solids are similar. Find the surface area of the red solid. *(Section 8.4)* 





- **9. HAMSTER** A hamster toy is in the shape of a sphere. What is the volume of the toy? Round your answer to the nearest whole number. *(Section 8.3)*
- **10. JEWELRY BOXES** The ratio of the corresponding linear measures of two similar jewelry boxes is 2 to 3. The larger box has a volume of 162 cubic inches. Find the volume of the smaller jewelry box. *(Section 8.4)*
- **11. ARCADE** You win a token after playing an arcade game. What is the volume of the gold ring? Round your answer to the nearest tenth. *(Section 8.3)*





### **Review Key Vocabulary**

sphere, <i>p. 348</i> hemisphere, <i>p. 351</i> similar solids, <i>p. 356</i>	sphere, <i>p. 348</i>	hemisphere, p. 351	similar solids, p. 356
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### **Review Examples and Exercises**



### Find the volume of the cylinder. Round your answer to the nearest tenth.



# Find the missing dimension of the cylinder. Round your answer to the nearest whole number.

- 5. Volume =  $25 \text{ in.}^3$
- **6.** Volume =  $7599 \text{ m}^3$



### 8.2 **Volumes of Cones** (pp. 340–345)



#### Exercises

Find the volume V or height h of the cone. Round your answer to the nearest tenth.





5 ft

9 ft

12 ft

9 ft

12 ft

Square Prism	Cylinder
V = Bh	V = Bh
= (12)(12)(9)	$=\pi(5)^{2}(9)$
= 1296	$= 225 \pi \approx 706.9$

So, the volume is about 1296 + 706.9 = 2002.9 cubic feet.

### Exercises

Find the volume V or radius r of the sphere. Round your answer to the nearest tenth, if necessary.



Find the volume of the composite solid. Round your answer to the nearest tenth.





The cones are similar. What is the volume of the red cone? Round your answer to the nearest tenth.



Volume =  $4608 \text{ m}^3$ 

# 8 Chapter Test



Find the volume of the solid. Round your answer to the nearest tenth.



- About how much more?
  CONES The ratio of the corresponding linear measures of two similar cones
- **7. CONES** The ratio of the corresponding linear measures of two similar cone is 3 to 4. The smaller cone has a volume of about 18 cubic inches. Find the volume of the larger cone. Round your answer to the nearest tenth.
- **8. OPEN-ENDED** Draw two different composite solids that have the same volume but different surface areas. Explain your reasoning.
- **9. MILK** Glass A has a diameter of 3.5 inches and a height of 4 inches. Glass B has a radius of 1.5 inches and a height of 5 inches. Which glass can hold more milk?
- **10. REASONING** Without calculating, determine which solid has the greater volume. Explain your reasoning.





### **Standards Assessment**

**1.** What value of *w* makes the equation below true? (8.*EE*.7*b*)

$$\frac{w}{3} = 3(w-1) - 1$$

A. 
$$\frac{1}{2}$$
 C.  $\frac{5}{4}$ 

 B.  $\frac{3}{4}$ 
 D.  $\frac{3}{2}$ 

2. A right circular cone and its dimensions are shown below.





What is the volume of the right circular cone?  $\left(\text{Use } \frac{22}{7} \text{ for } \pi.\right)$  (8.G.9)

- **H**  $4\,106^{2}\,\mathrm{cm}^{3}$ **F.**  $1,026\frac{2}{3}$  cm<sup>3</sup>
- **G.**  $3,080 \text{ cm}^3$

- I.  $12,320 \text{ cm}^3$
- **3.** Patricia solved the equation in the box shown.

What should Patricia do to correct the error that she made? (8.EE.7b)

- **A.** Add 10 to −20.
- **B.** Distribute  $-\frac{3}{2}$  to get -12x 15.
- **C.** Multiply both sides by  $-\frac{2}{3}$  instead of  $-\frac{3}{2}$ .

**D.** Multiply both sides by  $\frac{3}{2}$  instead of  $-\frac{3}{2}$ .

$$-\frac{3}{2}(8x - 10) = -20$$
$$8x - 10 = -20\left(-\frac{3}{2}\right)$$
$$8x - 10 = 30$$
$$8x - 10 + 10 = 30 + 10$$
$$8x = 40$$
$$\frac{8x}{8} = \frac{40}{8}$$
$$x = 5$$

**4.** On the grid below, Rectangle *EFGH* is plotted and its vertices are labeled.

		Ε	,	y			F		
(-	-1,	2)	1				(3,	2)	
-			1						_
-3	3 -2	2	0	1	12	2	4	1 5	5x
		Н					G		
(	(–1	, -	3)				(3,	-3	3)
			١	r					

Which of the following shows Rectangle E'F'G'H', the image of Rectangle EFGHafter it is reflected in the *x*-axis? (8.G.3)



5. List the ordered pairs shown in the mapping diagram below. (8.F.1)



- **B.** (2, -7), (4, -2), (6, 1), (8, 5)
- **C.** (2, 5), (4, 1), (6, -2), (8, -7)
- **D.** (5, 2), (-2, 4), (-7, 6), (1, 8)
- 6. The temperature fell from 54 degrees Fahrenheit to 36 degrees Fahrenheit over a 6-hour period. The temperature fell by the same number of degrees each hour. How many degrees Fahrenheit did the temperature fall each hour? (8.EE.7b)

**7.** Solve the formula below for *I*. (8.EE.7b)

$$A = P + PI$$
  
**F.**  $I = A - 2P$   
**H.**  $I = A - \frac{P}{P}$   
**G.**  $I = \frac{A}{P} - P$   
**I.**  $I = \frac{A - P}{P}$ 



**8.** A right circular cylinder has a volume of 1296 cubic inches. If you divide the radius of the cylinder by 12, what would be the volume, in cubic inches, of the smaller cylinder? (8.G.9)

**9.** Which graph represents a linear function? (8.F.3)





**10.** The figure below is a diagram for making a tin lantern.





The figure consists of a right circular cylinder without its top base and a right circular cone without its base. What is the volume, in cubic inches, of the entire lantern? Show your work and explain your reasoning. (Use 3.14 for  $\pi$ .) (8.*G*.9)