### 6.2 Representations of functions

## Essential Question how can you represent a function in <br> different ways?

## 1 ACTIVIIY: Describing a Function

Work with a partner. Copy and complete the mapping diagram for the area of the figure. Then write an equation that describes the function.
a.

b.



## 2 ACTIVIIY: Using a Jable

## Functions

In this lesson, you will

- write function rules.
- use input-output tables to represent functions.
- use graphs to represent functions.

Work with a partner. Make a table that shows the pattern for the area, where the input is the figure number $x$ and the output is the area $A$. Write an equation that describes the function. Then use your equation to find which figure has an area of 81 when the pattern continues.
a.

b.


## 3 ACJIVIJY: Using a Graph

Wath Practice
Construct Arguments
How does the graph help you determine whether the statement is true?

Work with a partner. Graph the data. Use the graph to test the truth of each statement. If the statement is true, write an equation that shows how to obtain one measurement from the other measurement.

a. "You can find the horsepower of a race car engine if you know its volume in cubic inches."

| Volume (cubic inches), $\boldsymbol{x}$ | 200 | 350 | 350 | 500 |
| :--- | :--- | :--- | :--- | :--- |
| Horsepower, $\boldsymbol{y}$ | 375 | 650 | 250 | 600 |

b. "You can find the volume of a race car engine in cubic centimeters if you know its volume in cubic inches."

| Volume (cubic inches), $x$ | 100 | 200 | 300 |
| :--- | :---: | :---: | :---: |
| Volume (cubic centimeters), $\boldsymbol{y}$ | 1640 | 3280 | 4920 |

## 4 ACJIV/JY: Interpreting a Graph

Work with a partner. The table shows the average speeds of the winners of the Daytona 500. Graph the data. Can you use the graph to predict future winning speeds? Explain why or why not.

| Year, $\boldsymbol{x}$ | 2004 | 2005 | 2006 | 2007 | 2008 | 2009 | 2010 | 2011 | 2012 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Speed (mi/h), $\boldsymbol{y}$ | 156 | 135 | 143 | 149 | 153 | 133 | 137 | 130 | 140 |

## What is Your Answer?

5. IN YOUR OWN WORDS How can you represent a function in different ways?

"I graphed our profits."

"And I am happy to say that they are going up every day!"

## Practice

Use what you learned about representing functions to complete Exercises 4-6 on page 253.

## Key Vocabulary (4)

function rule, p. 250

## Remember

An independent variable represents a quantity that can change freely. A dependent variable depends on the independent variable.

## © 50 Key Idea

## Functions as Equations

A function rule is an equation that describes the relationship between inputs (independent variable) and outputs (dependent variable).


EXAMPLE (1) Writing Function Rules
a. Write a function rule for "The output is five less than the input."

Words The output is five less than the input.
Equation $y=x-5$
$\therefore$ A function rule is $y=x-5$.
b. Write a function rule for "The output is the square of the input."

Words The output is the square of the input.
Equation $y=x^{2}$
$\because$ A function rule is $y=x^{2}$.

## EXAMPLE Evaluating a Function

What is the value of $y=2 x+5$ when $x=3$ ?

| $y$ | $=2 x+5$ |  | Write the equation. |
| ---: | :--- | ---: | :--- |
|  | $=2(3)+5$ |  | Substitute 3 for $x$. |
|  | $=11$ |  | Simplify. |

$\therefore \quad$ When $x=3, y=11$.

## On Your Own

1. Write a function rule for "The output is one-fourth of the input."

Find the value of $y$ when $x=5$.
2. $y=4 x-1$
3. $y=10 x$
4. $y=7-3 x$

## ©O Key Idea

Functions as Tables and Graphs
A function can be represented by an input-output table and by a graph. The table and graph below represent the function $y=x+2$.

| Input, <br> $\boldsymbol{x}$ | Output, <br> $\boldsymbol{y}$ | Ordered Pair, <br> $(\boldsymbol{x}, \boldsymbol{y})$ |
| :---: | :---: | :---: |
| 1 | 3 | $(1,3)$ |
| 2 | 4 | $(2,4)$ |
| 3 | 5 | $(3,5)$ |



By drawing a line through the points, you graph all of the solutions of the function $y=x+2$.

## EXAMPLE

## 3 Graphing a Function

Graph the function $y=-2 x+1$ using inputs of $-1,0,1$, and 2.
Make an input-output table.

| Input, $\boldsymbol{x}$ | $\mathbf{- 2 \boldsymbol { x } + \mathbf { 1 }}$ | Output, $\boldsymbol{y}$ | Ordered Pair, $(\boldsymbol{x}, \boldsymbol{y})$ |
| :---: | :---: | :---: | :---: |
| -1 | $-2(-1)+1$ | 3 | $(-1,3)$ |
| 0 | $-2(0)+1$ | 1 | $(0,1)$ |
| 1 | $-2(1)+1$ | -1 | $(1,-1)$ |
| 2 | $-2(2)+1$ | -3 | $(2,-3)$ |

Plot the ordered pairs and draw a line through the points.


## On Your Own

Exercises 19-24

Graph the function.
5. $y=x+1$
6. $y=-3 x$
7. $y=3 x+2$

## EXAMPLE <br> (4) Real-Life Application

The number of pounds $p$ of carbon dioxide produced by a car is 20 times the number of gallons $g$ of gasoline used by the car. Write and graph a function that describes the relationship between $g$ and $p$.

Write a function rule using the variables $g$ and $p$.
Words The number of pounds is 20 times the number of gallons of carbon dioxide of gasoline used.

$$
\begin{array}{llll}
\text { Equation } & p & =20 & \bullet
\end{array}
$$

Make an input-output table that represents the function $p=20 \mathrm{~g}$.

| Input, $\boldsymbol{g}$ | $\mathbf{2 0} \boldsymbol{g}$ | Output, $\boldsymbol{p}$ | Ordered Pair, (g, p) |
| :---: | :---: | :---: | :---: |
| 1 | $20(1)$ | 20 | $(1,20)$ |
| 2 | $20(2)$ | 40 | $(2,40)$ |
| 3 | $20(3)$ | 60 | $(3,60)$ |

Plot the ordered pairs and draw a line through the points.

Because you cannot have a negative number of gallons, use only positive values of $g$.


Gasoline (gallons)

## Now You're Ready

 Exercise 26
## On Your Own

8. WHAT IF? For a truck, $p$ is 25 times $g$. Write and graph a function that describes the relationship between $g$ and $p$.

## Co Summary

## Representations of Functions

Words An output is 2 more than the input.
Equation $y=x+2$
Input-Output Table

| Input, $\boldsymbol{x}$ | Output, $\boldsymbol{y}$ |
| :---: | :---: |
| -1 | 1 |
| 0 | 2 |
| 1 | 3 |
| 2 | 4 |

Mapping Diagram


Graph


## Vocabulary and Concept Check

1. VOCABULARY Identify the input variable and the output variable for the function rule $y=2 x+5$.
2. WRITING Describe five ways to represent a function.
3. DIFFERENT WORDS, SAME QUESTION Which is different? Find "both" answers.

What output is 4 more than twice the input 3 ?

What output is the sum of 2 times the input 3 and 4 ?

What output is twice the sum of the input 3 and 4 ?

What output is 4 increased by twice the input 3 ?

## Practice and Problem Solving

Write an equation that describes the function.
4.

5.

| Input, $\boldsymbol{x}$ | Output, $\boldsymbol{y}$ |
| :---: | :---: |
| 1 | 8 |
| 2 | 9 |
| 3 | 10 |
| 4 | 11 |

6. 

| Input, $\boldsymbol{x}$ | Output, $\boldsymbol{y}$ |
| :---: | :---: |
| 1 | 0 |
| 3 | -2 |
| 5 | -4 |
| 7 | -6 |

## Write a function rule for the statement.

(1) 7. The output is half of the input.
9. The output is three less than the input.
11. The output is six times the input.
12. The output is one more than twice the input.

Find the value of $\boldsymbol{y}$ for the given value of $\boldsymbol{x}$.
(2) 13. $y=x+5 ; x=3$
14. $y=7 x ; x=-5$
15. $y=1-2 x ; x=9$
16. $y=3 x+2 ; x=0.5$
17. $y=2 x^{3} ; x=3$
18. $y=\frac{x}{2}+9 ; x=-12$

## Graph the function.

(3)
19. $y=x+4$
20. $y=2 x$
21. $y=-5 x+3$
22. $y=\frac{x}{4}$
23. $y=\frac{3}{2} x+1$
24. $y=1+0.5 x$
25. ERROR ANALYSIS Describe and correct the error in graphing the function represented by the input-output table.

| Input, $x$ | -4 | -2 | 0 | 2 |
| :--- | :---: | :---: | :---: | :---: |
| Output, $\boldsymbol{y}$ | -1 | 1 | 3 | 5 |


(4) 26. DOLPHIN A dolphin eats 30 pounds of fish per day.
a. Write and graph a function that relates the number of pounds $p$ of fish that a dolphin eats in $d$ days.
b. How many pounds of fish does a dolphin eat in 30 days?

Match the graph with the function it represents.
27.

A. $y=\frac{x}{3}$
28.

B. $y=x+1$
29.

C. $y=-2 x+6$

Find the value of $\boldsymbol{x}$ for the given value of $\boldsymbol{y}$.
30. $y=5 x-7 ; y=-22$
31. $y=9-7 x ; y=37$
32. $y=\frac{x}{4}-7 ; y=2$
33. BRACELETS You decide to make and sell bracelets. The cost of your materials is $\$ 84$. You charge $\$ 3.50$ for each bracelet.
a. Write a function that represents the profit $P$ for selling $b$ bracelets.
b. Which variable is independent? dependent? Explain.
c. You will break even when the cost of your materials equals your income. How many bracelets must you
 sell to break even?
34. SALE A furniture store is having a sale where everything is $40 \%$ off.
a. Write a function that represents the amount of discount $d$ on an item with a regular price $p$.
b. Graph the function using the inputs $100,200,300,400$, and 500 for $p$.
c. You buy a bookshelf that has a regular price of $\$ 85$. What is the sale price of the bookshelf?

35. AIRBOAT TOURS You want to take a two-hour airboat tour.
a. Write a function that represents the cost $G$ of a tour at Gator Tours.
b. Write a function that represents the cost $S$ of a tour at Snake Tours.
c. Which is a better deal? Explain.

36. REASONING The graph of a function is a line that goes through the points $(3,2),(5,8)$, and $(8, y)$. What is the value of $y$ ?
37. CRITICAL THINKING Make a table where the independent variable is the side length of a square and the dependent variable is the perimeter. Make a second table where the independent variable is the side length of a square and the dependent variable is the area. Graph both functions in the same coordinate plane. Compare the functions and graphs.
38. Puzzle The blocks that form the diagonals of each square are shaded. Each block is one square unit. Find the "green area" of Square 20. Find the "green area" of Square 21. Explain your reasoning.


Square 1


Square 2


Square 3


Square 4


Square 5

## Fair Game Review what you learned in previous grades \& lessons

Find the slope of the line. (Section 4.2)
39.

40.

41.

42. MULTIPLE CHOICE You want to volunteer for at most 20 hours each month. So far, you have volunteered for 7 hours this month. Which inequality represents the number of hours $h$ you can volunteer for the rest of this month? (Skills Review Handbook)
(A) $h \geq 13$
(B) $h \geq 27$
(C) $h \leq 13$
(D) $h<27$

